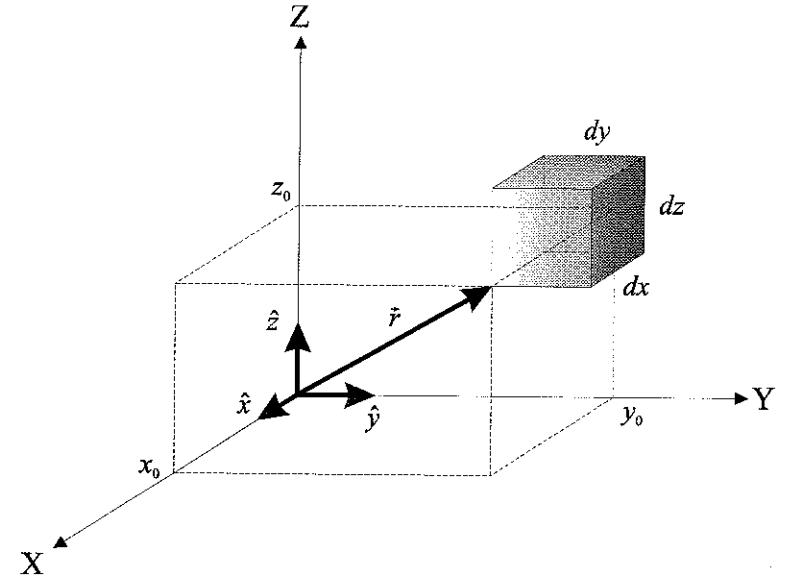
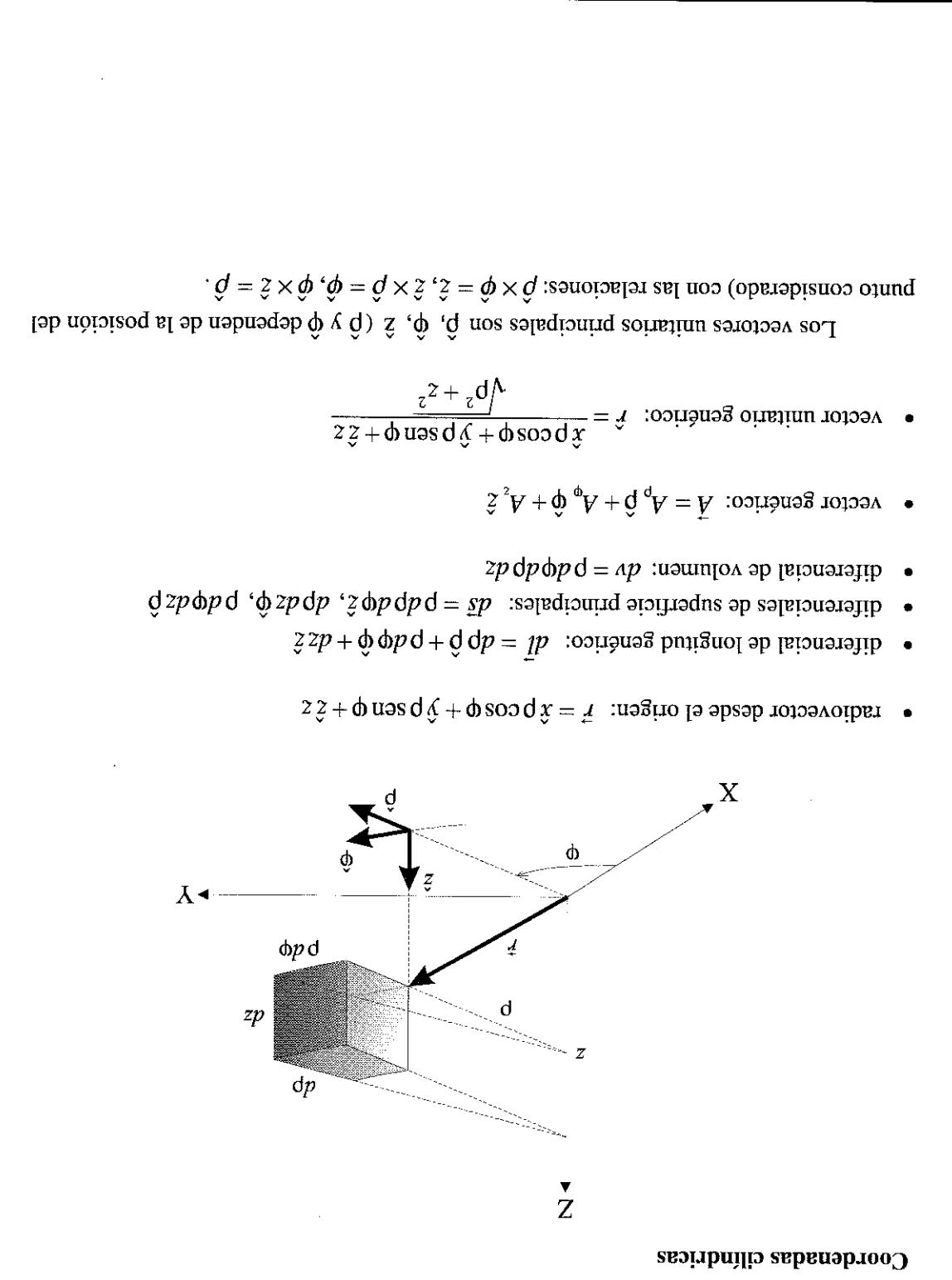
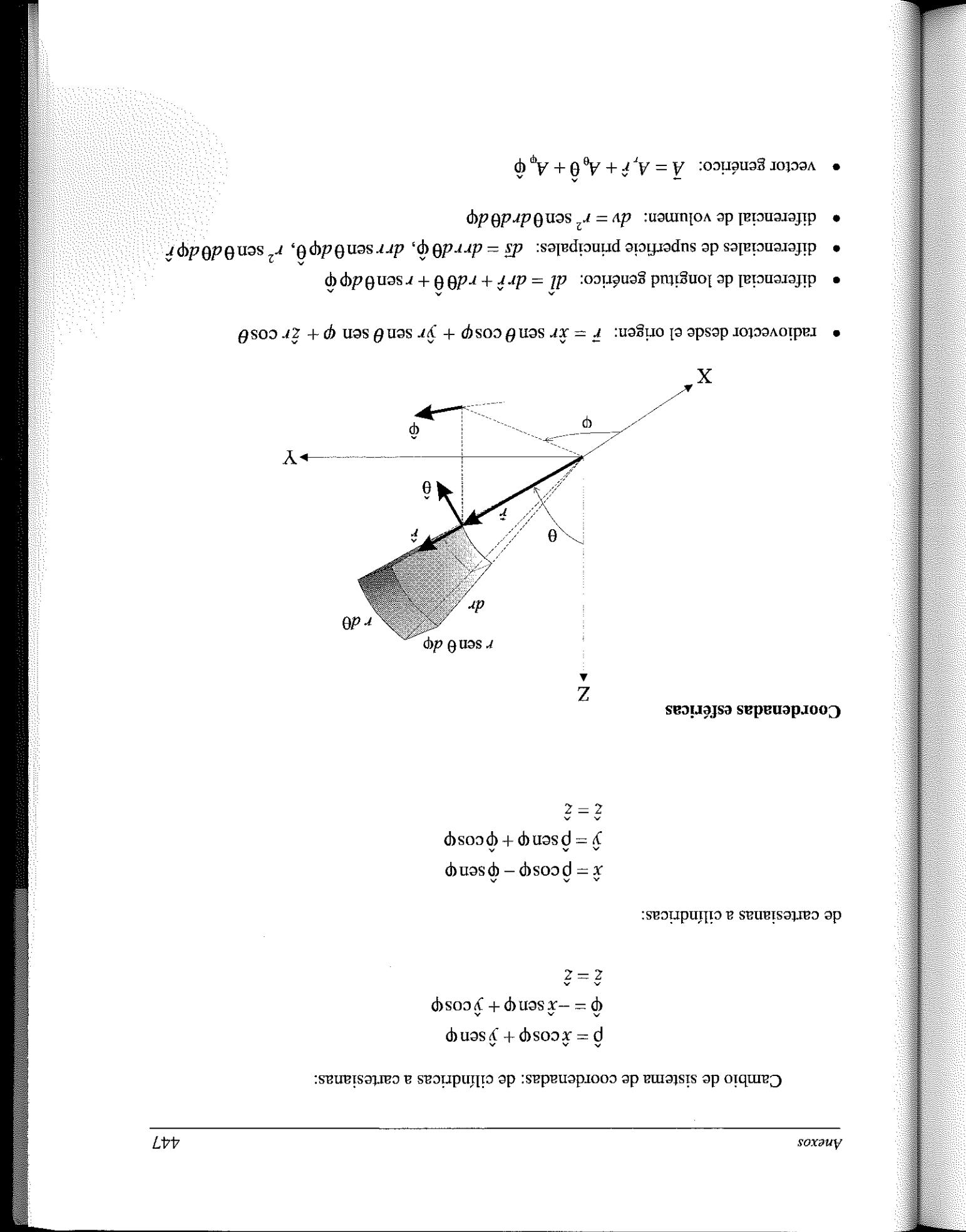


Anexo A: Sistemas de coordenadas

Coordenadas rectangulares



- radiovector desde el origen: $\vec{r} = x_0 \hat{x} + y_0 \hat{y} + z_0 \hat{z}$
- diferencial de longitud genérico: $d\vec{l} = dx \hat{x} + dy \hat{y} + dz \hat{z}$
- diferenciales de superficie principales: $d\vec{s} = dx dy \hat{z}$, $dx dz \hat{y}$, $dy dz \hat{x}$
- diferencial de volumen: $dv = dx dy dz$
- vector genérico: $\vec{A} = A_x \hat{x} + A_y \hat{y} + A_z \hat{z}$
- vector unitario genérico: $\hat{r} = \frac{x \hat{x} + y \hat{y} + z \hat{z}}{\sqrt{x^2 + y^2 + z^2}}$



- Vector unitario genérico: $\hat{r} = \frac{r \operatorname{sen} \theta \cos \phi \hat{x} + r \operatorname{sen} \theta \operatorname{sen} \phi \hat{y} + r \cos \theta \hat{z}}{r}$

Camps electromagnètics

Los vectores unitarios principales son $\hat{r}, \hat{\theta}, \hat{\phi}$ (todos ellos dependientes de la posición del punto en que se consideran) con las relaciones:

$$\begin{aligned}\hat{r} &= \hat{x} \operatorname{sen} \theta \cos \phi + \hat{y} \operatorname{sen} \theta \operatorname{sen} \phi + \hat{z} \cos \theta \\ \hat{\theta} &= \hat{x} \cos \theta \cos \phi + \hat{y} \cos \theta \operatorname{sen} \phi - \hat{z} \operatorname{sen} \theta \\ \hat{\phi} &= -\hat{x} \operatorname{sen} \phi + \hat{y} \cos \phi\end{aligned}$$

$$\begin{aligned}x &= r \operatorname{sen} \theta \operatorname{sen} \phi + \theta \cos \theta \operatorname{sen} \phi + \phi \cos \theta \\ y &= r \operatorname{sen} \theta \cos \phi + \theta \cos \theta \cos \phi - \phi \operatorname{sen} \theta \\ z &= r \cos \theta - \theta \operatorname{sen} \theta\end{aligned}$$

de cartesianas a esféricas:

$$\begin{aligned}\Delta^2 A &= \Delta_x^2 A + \Delta_y^2 A + \Delta_z^2 A = (\Delta_x A)^2 + (\Delta_y A)^2 + (\Delta_z A)^2 \\ \Delta \cdot A &= \frac{\partial}{\partial x} \left(\frac{\partial A}{\partial x} \right) + \frac{\partial}{\partial y} \left(\frac{\partial A}{\partial y} \right) + \frac{\partial}{\partial z} \left(\frac{\partial A}{\partial z} \right) \\ \Delta \times A &= \frac{\partial}{\partial x} \left(\frac{\partial A}{\partial y} - \frac{\partial A}{\partial z} \right) + \frac{\partial}{\partial y} \left(\frac{\partial A}{\partial z} - \frac{\partial A}{\partial x} \right) + \frac{\partial}{\partial z} \left(\frac{\partial A}{\partial x} - \frac{\partial A}{\partial y} \right)\end{aligned}$$

Coordenadas rectangulares

Operadores

$$\begin{aligned}\frac{\partial}{\partial x} &= \frac{\partial}{\partial r} \frac{\partial r}{\partial x} + \frac{\partial}{\partial \theta} \frac{\partial \theta}{\partial x} + \frac{\partial}{\partial \phi} \frac{\partial \phi}{\partial x} \\ \frac{\partial}{\partial y} &= \frac{\partial}{\partial r} \frac{\partial r}{\partial y} + \frac{\partial}{\partial \theta} \frac{\partial \theta}{\partial y} + \frac{\partial}{\partial \phi} \frac{\partial \phi}{\partial y} \\ \frac{\partial}{\partial z} &= \frac{\partial}{\partial r} \frac{\partial r}{\partial z} + \frac{\partial}{\partial \theta} \frac{\partial \theta}{\partial z} + \frac{\partial}{\partial \phi} \frac{\partial \phi}{\partial z} \\ \Delta &= \frac{\partial^2}{\partial r^2} + \frac{1}{r^2} \frac{\partial^2}{\partial \theta^2} + \frac{1}{r^2 \sin^2 \theta} \frac{\partial^2}{\partial \phi^2}\end{aligned}$$

Coordenadas cilíndricas

$$\begin{aligned}\Delta^2 A &= \Delta_r^2 A + \Delta_\theta^2 A + \Delta_\phi^2 A = (\Delta_r A)^2 + (\Delta_\theta A)^2 + (\Delta_\phi A)^2 \\ \Delta \cdot A &= \frac{\partial}{\partial r} \left(\frac{\partial A}{\partial r} \right) + \frac{1}{r^2} \frac{\partial}{\partial \theta} \left(\frac{\partial A}{\partial \theta} \right) + \frac{1}{r^2 \sin^2 \theta} \frac{\partial}{\partial \phi} \left(\frac{\partial A}{\partial \phi} \right) \\ \Delta \times A &= \frac{\partial}{\partial r} \left(\frac{\partial A}{\partial \theta} - \frac{\partial A}{\partial \phi} \right) + \frac{1}{r^2} \frac{\partial}{\partial \theta} \left(\frac{\partial A}{\partial \phi} - \frac{\partial A}{\partial r} \right) + \frac{1}{r^2 \sin^2 \theta} \frac{\partial}{\partial \phi} \left(\frac{\partial A}{\partial r} - \frac{\partial A}{\partial \theta} \right)\end{aligned}$$

Coordenadas rectangulares

Operadores

Anexo B: Formulas de análisis vectorial